



**Second Midterm Examination
Summer Semester 2025 - 2026**

July 13, 2026

Time: 6:30 PM –8:00 PM

Name: Student No:

Section No: Serial No:

Instructors: Drs. Abdul Mohsen, Alaa, Elias, Peter, & Yahya

Fundamental constants

$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ N}\cdot\text{m}^2 / \text{C}^2$	(Coulomb constant)
$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N} \cdot \text{m}^2)$	(Permittivity of free space)
$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$	(Permeability of free space)
$ e = 1.60 \times 10^{-19} \text{ C}$	(Elementary unit of charge)
$N_A = 6.02 \times 10^{23}$	(Avogadro's number)
$g = 9.8 \text{ m/s}^2$	(Acceleration due to gravity)
$m_e = 9.11 \times 10^{-31} \text{ kg}$	(Electron mass)
$m_p = 1.67 \times 10^{-27} \text{ kg}$	(Proton mass)

Prefixes of units

$m = 10^{-3}$	$\mu = 10^{-6}$	$n = 10^{-9}$	$p = 10^{-12}$
$k = 10^3$	$M = 10^6$	$G = 10^9$	$T = 10^{12}$

For use by Instructors only

Problems	1	2	3	4	5	6	Questions	Total
Marks								

Instructions to the Students:

1. Mobile or other electronic devices are **strictly prohibited** during the exam.
2. Programmable calculators, which can store equations, are not allowed.
3. Cheating incidents will be processed according to the university rules.

PART I: Solve the following problems. Show your solutions in detail.

1. A conducting sphere of radius $R = 0.30$ m and charge $Q_1 = 60$ nC is centered at the origin, as shown. A point charge $q = -20$ nC is placed on the x -axis, as shown, and a uniformly charged ring of charge $Q_2 = -40$ nC and radius $a = 0.60$ m has its symmetry axis aligned with the x -axis. If $V = 0$ at infinity, find the electric potential at the origin. **[5 points]**

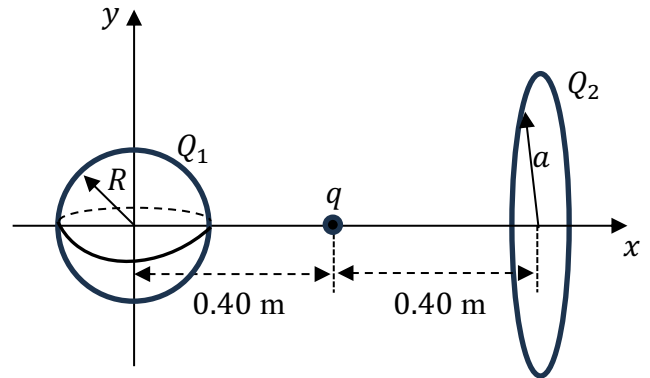
$$V_{\text{sphere}} = k \frac{Q_1}{R} \Rightarrow V_{\text{sphere}} = +1800 \text{ V}$$

$$V_q = k \frac{q}{0.40} \Rightarrow V_q = -450 \text{ V}$$

$$V_{\text{ring}} = k \frac{Q_2}{\sqrt{(0.80)^2 + (0.60)^2}} \Rightarrow V_{\text{ring}} = -360 \text{ V}$$

$$V_{\text{origin}} = V_{\text{sphere}} + V_q + V_{\text{ring}}$$

$$V_{\text{origin}} = 990 \text{ V}$$



2. In the given network of capacitors, $C_1 = 7$ nF, $C_2 = 3$ nF, $C_3 = 6$ nF, and $C_4 = 9$ nF. The network of capacitors is charged by a potential difference V and the electric energy stored in the capacitor C_3 is 15 nJ. Find the electric charge stored on capacitor C_1 . **[5 points]**

$$U_3 = \frac{1}{2} C_3 V_3^2 \Rightarrow V_3 = \frac{2U_3}{C_3} \Rightarrow V_3 = 2.236 \text{ V}$$

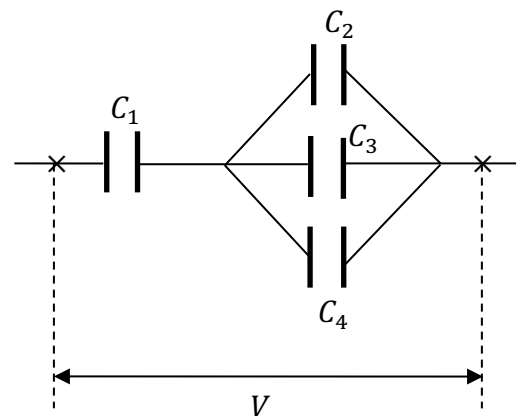
$$V_3 = V_2 = V_4 = V_{234} \Rightarrow V_{234} = 2.236 \text{ V}$$

$$C_{234} = C_2 + C_3 + C_4 \Rightarrow C_{234} = 18 \text{ nF}$$

$$C_{234} = \frac{Q_{234}}{V_{234}} \Rightarrow Q_{234} = C_{234} V_{234} \Rightarrow Q_{234} = 40.248 \text{ nC}$$

Since Q_1 and Q_{234} in series:

$$Q_{234} = Q_1 \Rightarrow Q_1 = 40.248 \text{ nC}$$



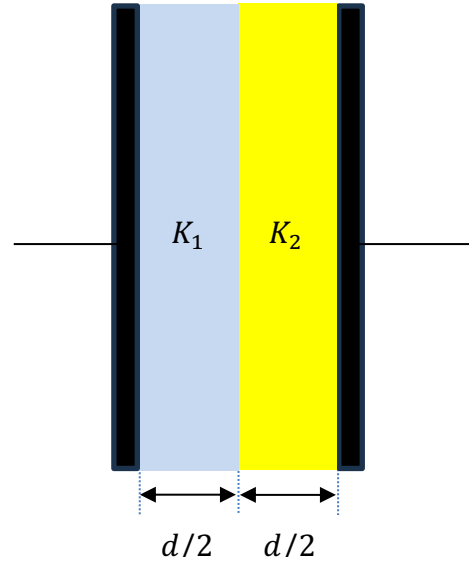
3. An air-filled parallel-plate capacitor with surface area A and plate separation d , has capacitance $C_0 = 30 \mu\text{F}$. Then, the capacitor is filled with two dielectric slabs of dielectric constants $K_1 = 5$ and $K_2 = 7$, filling each one of them the $1/2$ of the space between the plates, as shown. Calculate the capacitance of this capacitor. **[4 points]**

$$C_0 = \epsilon_0 \frac{A}{d}$$

$$C_1 = K_1 \epsilon_0 \frac{A}{d/2} \Rightarrow C_1 = 10C_0 \Rightarrow C_1 = 300 \mu\text{F}$$

$$C_2 = K_2 \epsilon_0 \frac{A}{d/2} \Rightarrow C_2 = 14C_0 \Rightarrow C_2 = 420 \mu\text{F}$$

$$\frac{1}{C_{eq}} = \frac{1}{C_1} + \frac{1}{C_2} \Rightarrow C_{eq} = 175 \mu\text{F}$$



4. An electric current in a metallic wire varies with time as $I(t) = 20t - 0.005$ with electric current $I(t)$ in amperes and time t in seconds. Calculate the electric charge that passes through a cross section of the wire between time $t = 0$ s and $t = 1$ ms. **[4 points]**

$$I(t) = \frac{dQ}{dt} \Rightarrow dQ = I(t)dt$$

$$Q = \int_0^{1 \times 10^{-3}} I(t)dt$$

$$Q = \int_0^{1 \times 10^{-3}} (20t - 0.005)dt \Rightarrow Q = 20 \frac{t^2}{2} \Big|_0^{1 \times 10^{-3}} - 0.005 t \Big|_0^{1 \times 10^{-3}}$$

$$Q = 5 \mu\text{C}$$

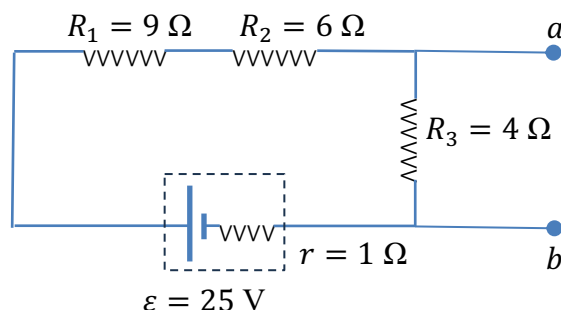
5. In the circuit below, find the potential difference, V_{ab} , between points a and b.

[3 points]

$$R_{eq} = R_1 + R_2 + R_3 + r \Rightarrow R_{eq} = 20 \Omega$$

$$I = \frac{\varepsilon}{R_{eq}} \Rightarrow I = 1.25 \text{ A}$$

$$V_{ab} = V_3 \Rightarrow V_{ab} = IR_3 \Rightarrow V_{ab} = 5 \text{ V}$$



6. In the circuit shown below, find the electric currents I_1 and I_2 .

[5 Points]

$$I_3 = I_1 + I_2$$

$$\varepsilon_1 - 5I_3 - 10I_1 = 0$$

$$10 - 15I_1 - 5I_2 = 0 \quad (1)$$

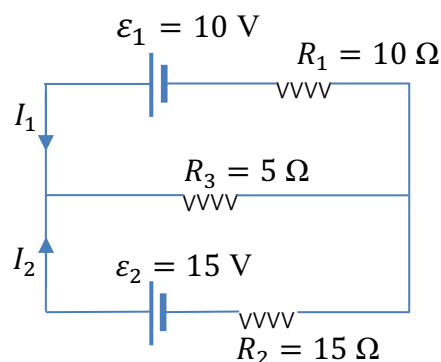
$$\varepsilon_2 - 5I_3 - 15I_2 = 0$$

$$15 - 5I_1 - 20I_2 = 0 \quad (2)$$

Multiply (2) with (-3): $-45 + 15I_1 + 60I_2 = 0 \quad (3)$

Add (3) to (1): $-35 + 55I_2 = 0 \Rightarrow I_2 = 0.636 \text{ A}$

$(1) \Rightarrow 10 - 15I_1 - 5 \times 0.636 = 0 \Rightarrow I_1 = 0.455 \text{ A}$



PART II: Conceptual Questions (each carries 1 point). Circle the best answer:

1. Which statement is correct?

- a) The equipotential surfaces are always parallel to the electric field lines.
- b) The equipotential surfaces are always flat surfaces.
- c) The equipotential surfaces are always perpendicular to the electric field lines. **(ANSWER)**
- d) The equipotential surfaces are always at angle 45° with the electric field lines.

2. A point charge $q < 0$ is released on the x -axis between points a and b and moves towards the point b . Therefore, the relation between the electric potential V_a at point a and the electric potential V_b at point b , is:



- a) $V_a = V_b$.
- b) $V_a > V_b$.
- c) $V_a < V_b$. **(ANSWER)**
- d) $V_a = V_b = 0$.

3. An air-filled parallel-plate capacitor with plate separation d , area A , and capacitance C_0 is charged by a battery V . The battery remains connected and a slab of dielectric material with dielectric constant K is inserted completely filling the space between the plates of the capacitor. Which statement is correct?

- a) The potential difference of the capacitor decreases by a factor of K .
- b) The potential difference of the capacitor increases by a factor of K .
- c) The electric potential energy decreases by a factor of K .
- d) The electric charge of the capacitor increases by a factor of K . **(ANSWER)**

4. An air-filled parallel-plate capacitor with plate separation d , area A , and capacitance C_0 is charged by a battery V . If the battery is disconnected and a slab of dielectric material with dielectric constant K is inserted completely filling the space between the plates of the capacitor, the energy density u

- a) decreases by a factor K . **(ANSWER)**
- b) increases by a factor K .
- c) decreases by a factor K^2 .
- d) remains the same.

5. The negative charges in a metallic wire are moving in the $(-\hat{j})$ direction. The electric current I and the current density J in the wire have directions:
- a) I is to $(+\hat{i})$ and J is to $(+\hat{i})$.
 - b) I is to $(+\hat{j})$ and J is to $(+\hat{j})$. **(ANSWER)**
 - c) I is to $(+\hat{i})$ and J is to $(-\hat{j})$.
 - d) I is to $(-\hat{i})$ and J is to $(+\hat{j})$.
6. A loop in an electric circuit is
- a) a point where three or more conductors (wires) meet.
 - b) any closed path in the circuit. **(ANSWER)**
 - c) any single path containing a circuit element between two junctions.
 - d) any closed path in the circuit that does not include an emf source.
7. Kirchhoff's loop rule follows from the fact that
- a) the electrostatic force is conservative. **(ANSWER)**
 - b) the electric charge is conserved.
 - c) the electric potential is the same everywhere in a circuit.
 - d) the electric potential energy is the same everywhere in a circuit.
8. A junction in a circuit is
- a) a closed conducting path.
 - b) a part of a closed conducting path
 - c) a point next to the source of emf.
 - d) a point where three or more conductors (wires) meet. **(ANSWER)**