



**Final Examination**  
**Summer Semester 2025 – 2026**

**July 27, 2026**

**Time: 6:00 – 8:00 PM**

Name: ..... Student ID: .....

Sec. No: ..... Serial No: .....

Instructors: Drs. Abdulmuhsen, Alaa, Elias, Peter, & Yahya

**Fundamental constants**

|                                                                               |                               |
|-------------------------------------------------------------------------------|-------------------------------|
| $k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ N.m}^2 / \text{C}^2$   | (Coulomb constant)            |
| $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N} \cdot \text{m}^2)$ | (Permittivity of free space)  |
| $\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$                      | (Permeability of free space)  |
| $ e  = 1.60 \times 10^{-19} \text{ C}$                                        | (Elementary unit of charge)   |
| $N_A = 6.02 \times 10^{23}$                                                   | (Avogadro's number)           |
| $g = 9.8 \text{ m/s}^2$                                                       | (Acceleration due to gravity) |
| $m_e = 9.11 \times 10^{-31} \text{ kg}$                                       | (Electron mass)               |
| $m_p = 1.67 \times 10^{-27} \text{ kg}$                                       | (Proton mass)                 |

**Prefixes of units**

|               |                 |               |                |
|---------------|-----------------|---------------|----------------|
| $m = 10^{-3}$ | $\mu = 10^{-6}$ | $n = 10^{-9}$ | $p = 10^{-12}$ |
| $k = 10^3$    | $M = 10^6$      | $G = 10^9$    | $T = 10^{12}$  |

**For use by Instructors only**

| Problems | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | Questions | Total |
|----------|---|---|---|---|---|---|---|---|-----------|-------|
| Marks    |   |   |   |   |   |   |   |   |           |       |

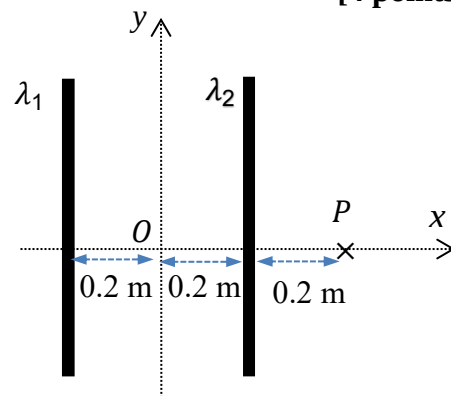
**Instructions to the Students:**

1. Mobile or other electronic devices are **strictly prohibited** during the exam.
2. Programmable calculators, which can store equations, are not allowed.
3. **Cheating incidents will be processed according to the university rules.**

**PART I: Solve the following problems. Show your solutions in detail.**

1. Two very long uniformly charged lines with linear charge densities  $\lambda_1 = 9 \text{ nC/m}$  and  $\lambda_2 = -9 \text{ nC/m}$  are fixed perpendicular to the  $x$ -axis, as shown. If a point charge  $q$  is placed at the origin,  $O$ , the net electric force acting on it is  $\vec{F} = -(2 \text{ N})\hat{i}$ . Calculate the net electric force acting on charge  $q$  when it is at point  $P$ .

[4 points]



$$\vec{F}_{net,O} = q\vec{E}_{net,O} = q \left( \frac{|\lambda_1|}{2\pi\epsilon_0 0.2\text{m}} + \frac{|\lambda_2|}{2\pi\epsilon_0 0.2\text{m}} \right) \hat{i}$$

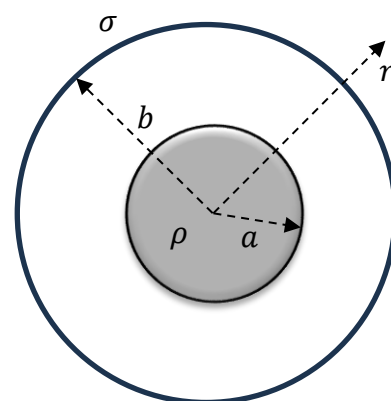
$$q \frac{|\lambda_1|}{2\pi\epsilon_0} \left( \frac{1}{0.2\text{m}} + \frac{1}{0.2\text{m}} \right) \hat{i} = -(2 \text{ N})\hat{i} \Rightarrow q = -1.24 \times 10^{-3} \text{ C}$$

$$\vec{F}_{net,P} = q\vec{E}_{net,P} = q \frac{|\lambda_1|}{2\pi\epsilon_0} \left( \frac{1}{0.6\text{m}} - \frac{1}{0.2\text{m}} \right) \hat{i} =$$

$$= -(2 \text{ N}) \left( \frac{1}{10} \right) \left( \frac{1}{0.6} - \frac{1}{0.2} \right) \hat{i} = (0.67 \text{ N})\hat{i}$$

2. A sphere of radius  $a = 5 \text{ cm}$  with a uniform volume charge density  $\rho = -6 \text{ } \mu\text{C/m}^3$  is inside a concentric thin conducting spherical shell of radius  $b = 10 \text{ cm}$  with uniform surface charge density  $\sigma = 12 \text{ nC/m}^2$ . Calculate the magnitude and direction of the net electric field  $\vec{E}$  at distance  $r = 14 \text{ cm}$  from the center.

[4 points]



$$\text{Gauss's Law: } \oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0} \Rightarrow$$

$$\pm E(4\pi r^2) = \frac{Q_{encl}}{\epsilon_0}$$

(The sign of the LHS is the same as the sign of the yet unknown  $Q_{encl}$ .)

$$Q_{encl} = \rho \frac{4\pi}{3} a^3 + \sigma 4\pi b^2 = -1.63 \text{ nC}$$

$$-E = \frac{Q_{encl}}{\epsilon_0 4\pi r^2} = -750 \text{ N/C,}$$

$$E = 750 \text{ N/C; inward}$$

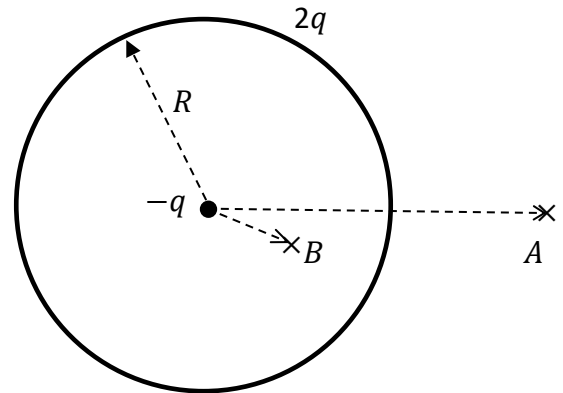
3. A spherical surface of radius  $R = 1.0$  m has charge  $2q$  uniformly distributed on it and a point charge  $-q$  is fixed at its centre. If  $V = 0$  at infinity, the electric potential at point  $A$  is 480 V. Point  $A$  is at distance  $r_A = 1.5$  m from the centre and point  $B$  is at distance  $r_B = 0.8$  m. What is the electric potential at point  $B$ ?

[4 points]

$$V_A = V_{-q,A} + V_{2q,A} \Rightarrow 480 \text{ V} = k \frac{-q}{r_A} + k \frac{2q}{r_A} \Rightarrow$$

$$q = 80 \text{ nC}$$

$$V_B = V_{-q,B} + V_{2q,B} = k \frac{-q}{r_B} + k \frac{2q}{R} = 540 \text{ V}$$



4. Two air-filled capacitors,  $C_1 = C_2$ , are connected to a battery,  $V = 24$  V, as shown, so the energy stored in the two capacitors is 80  $\mu$ J. Then, we fully fill the space between the plates of only  $C_2$  with a dielectric material of dielectric constant  $K$ , so the final energy stored in the two capacitors will be 240  $\mu$ J. Find the value of  $K$ .

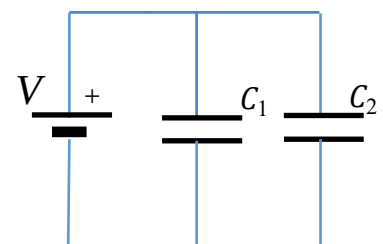
[4 points]

$$C_{eq} = C_1 + C_2 = 2C_1$$

$$U_{in} = \frac{C_{eq}V^2}{2} = 80 \mu\text{J}$$

$$U_{fin} = \frac{(C_1 + KC_1)V^2}{2} = 240 \mu\text{J} \Rightarrow$$

$$C_1 + KC_1 = 3(C_1 + C_1) \Rightarrow K = 5$$



5. A cylindrical metal wire has length  $L = 4$  m, radius  $r = 0.3$  mm and a potential difference  $V = 40$  V is applied between its ends. If the resistivity of the wire is  $18.7 \times 10^{-8} \Omega \cdot \text{m}$ , and the concentration of the free electrons is  $8.5 \times 10^{28} / \text{m}^3$ , how much time is required for an electron to travel the length of the wire? **[4 points]**

$$E = \frac{V}{L} = 10 \text{ V/m}$$

$$\rho = \frac{E}{J} \Rightarrow J = \frac{E}{\rho} = 5.3 \times 10^7 \text{ A/m}^2$$

$$J = nqv_d = nq\frac{L}{t} \Rightarrow$$

$$t = nq\frac{L}{J} = 1017 \text{ s}$$

6. In the circuit below, initially the capacitor is uncharged and the switch  $S$  is closed at time  $t = 0$  s. Find the current  $I$  in the circuit at time  $t_1$  at which the energy stored in the capacitor is  $\frac{4}{9}$  of its final value. **[5 points]**

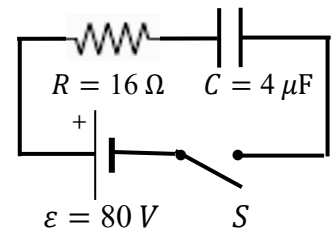
$$Q(t) = \varepsilon C \left[ 1 - e^{-\frac{t}{RC}} \right] \Rightarrow U(t) = \frac{Q^2}{2C} = \frac{(\varepsilon C)^2 \left[ 1 - e^{-\frac{t}{RC}} \right]^2}{2C}$$

$$U(\infty) = \frac{(\varepsilon C)^2}{2C} \Rightarrow \frac{4}{9} = \left[ 1 - e^{-\frac{t_1}{RC}} \right]^2$$

$$e^{-\frac{t_1}{RC}} = \frac{1}{3}$$

$$I(t) = \frac{dQ(t)}{dt} = \frac{\varepsilon}{R} e^{-\frac{t}{RC}}$$

$$I(t_1) = \frac{\varepsilon}{R} \frac{1}{3} = 1.67 \text{ A}$$



7. A proton moves momentarily with a velocity of  $\vec{v} = \left(4 \times 10^5 \frac{\text{m}}{\text{s}}\right)\hat{i} + \left(8 \times 10^5 \frac{\text{m}}{\text{s}}\right)\hat{j} + \left(3 \times 10^5 \frac{\text{m}}{\text{s}}\right)\hat{k}$  in a uniform magnetic field  $\vec{B} = B_y\hat{j}$ . If the radius of the helical path is  $R = 0.06 \text{ m}$ , what is the magnitude of  $B_y$ ? **[3 points]**

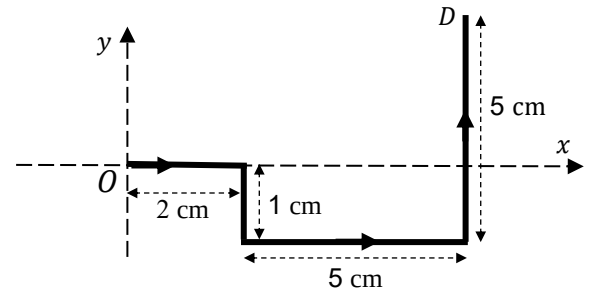
$$v_{\perp} = \sqrt{v_x^2 + v_z^2} = 5 \times 10^5 \frac{\text{m}}{\text{s}}$$

$$R = \frac{mv_{\perp}}{|q|B_y} = 0.06 \text{ m} \Rightarrow B_y = \frac{mv_{\perp}}{|q|R} = 0.087 \text{ T}$$

8. A 4-A current flows in the wire from point  $O$  to point  $D$ , as shown. Calculate the magnetic force vector acting on the wire by a uniform magnetic field  $\vec{B} = (6 \text{ T})\hat{i} + (4 \text{ T})\hat{j}$ . **[4 points]**

$$\vec{L}_{eff} = (0.07 \text{ m})\hat{i} + (0.04 \text{ m})\hat{j}$$

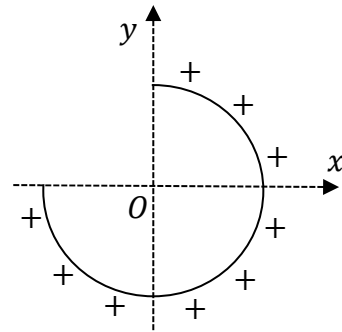
$$\begin{aligned}\vec{F}_B &= I\vec{L}_{eff} \times \vec{B} = \\ &= 4A[(0.07 \text{ m})\hat{i} + (0.04 \text{ m})\hat{j}] \times [(6 \text{ T})\hat{i} + (4 \text{ T})\hat{j}] \\ &= (1.12 \text{ N})\hat{k} - (0.96 \text{ N})\hat{k} = (0.16 \text{ N})\hat{k}\end{aligned}$$



**PART II: Conceptual Questions (each carries 1 point). Tick the best answer:**

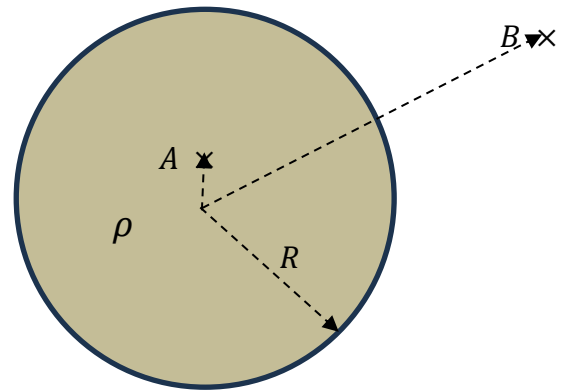
1. The circular arc in the figure is uniformly charged as shown. The direction of the net electric field at the origin is

- a)  $+\hat{i} + \hat{j}$ .
- b)  $-\hat{i} - \hat{j}$ .
- c)  $+\hat{i} - \hat{j}$ .
- d)  $-\hat{i} + \hat{j}$ .  $\Leftarrow$



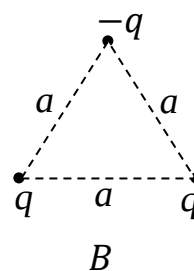
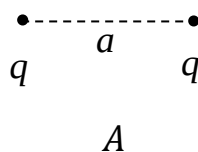
2. A uniformly charged insulating sphere has radius  $R$ . Point  $A$  is at distance  $R/4$ , and point  $B$  is at distance  $2R$  from the centre. Which relation is correct for the magnitude of electric fields at these points?

- a)  $E_A > E_B$ .
- b)  $E_A < E_B$ .
- c)  $E_A = E_B$ .  $\Leftarrow$
- d) If  $\rho < 0$ ,  $E_A > E_B$ ; otherwise  $E_A < E_B$ .



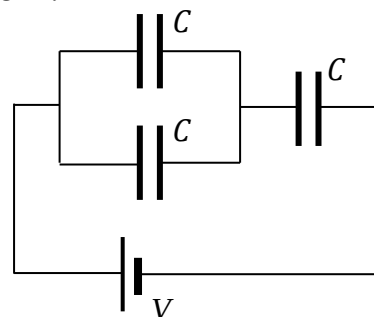
3. Two systems of charges  $A$  and  $B$  are made of identical magnitude of charges  $q$ , as shown. If the total potential energy of system  $A$  is  $U$ , the total potential energy of system  $B$  is

- a)  $U$ .
- b)  $-U$ .  $\Leftarrow$
- c)  $3U$ .
- d)  $-3U$ .



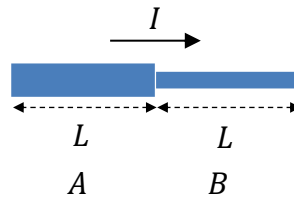
4. Three identical capacitors are connected into a network as shown. Which statement is correct for the equivalent capacitance,  $C_{eq}$ , of the network?

- a)  $C_{eq} < C$ .  $\Leftarrow$
- b)  $C_{eq} > C$ .
- c)  $C_{eq} = C$ .
- d) There is not enough information to decide.



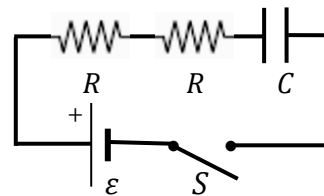
5. Cylindrical wire  $A$  has length  $L$ , radius  $2r$ . Cylindrical wire  $B$  is made of the same material, and has length  $L$ , radius  $r$ . These wires are welded together at their ends and a current  $I$  flows in them as shown. The magnitude of electric field in wire  $B$  is

- a) larger than in wire  $A$ .  $\Leftarrow$
- b) smaller than in wire  $A$ .
- c) the same as in wire  $A$ .
- d) zero.



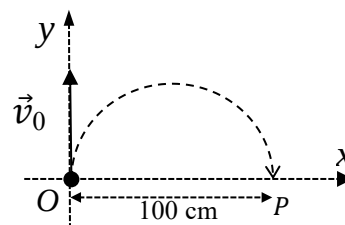
6. In the  $R$ - $C$  circuit below the capacitor is originally uncharged and the switch  $S$  is closed at time  $t = 0$  s. The initial current in the circuit is

- a)  $I_0 = \frac{\varepsilon}{R}$ .
- b)  $I_0 = \frac{2\varepsilon}{R}$
- c)  $I_0 = \frac{\varepsilon}{2R}$ .  $\Leftarrow$
- d) 0.



7. At point  $O$ , a proton has a velocity  $\vec{v}_0 = v_0 \hat{j}$ . Find the direction of the uniform magnetic field that will make the proton to move on a semi-circular path from point  $O$  to point  $P$

- a)  $\hat{j}$ .
- b)  $\hat{k}$ .  $\Leftarrow$
- c)  $-\hat{k}$ .
- d)  $-\hat{i}$ .



8. In a velocity selector the magnitude of the uniform electric field is  $E$  and the magnitude of the uniform magnetic field is  $B$ . If a charged particle moves through the region of perpendicular magnetic and electric fields along a straight line, it has a speed of

- a)  $v = \frac{B}{E}$ .
- b)  $v = \frac{E}{B}$ .  $\Leftarrow$
- c)  $v = \frac{B^2}{E^2}$ .
- d)  $v = 0$ .