


Second Midterm Examination
Spring Semester 2025 - 2026
April 18, 2026
Time: 3:30 PM – 5:00 PM

Name: Student No:

Section No: Serial No:

Instructors: Drs. Abdullah, Ali, Al-Mumin, Lajko, Sharma, & Vagenas

Fundamental constants

$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ N}\cdot\text{m}^2 / \text{C}^2$	(Coulomb constant)
$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N} \cdot \text{m}^2)$	(Permittivity of free space)
$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A}$	(Permeability of free space)
$ e = 1.60 \times 10^{-19} \text{ C}$	(Elementary unit of charge)
$N_A = 6.02 \times 10^{23}$	(Avogadro's number)
$g = 9.8 \text{ m/s}^2$	(Acceleration due to gravity)
$m_e = 9.11 \times 10^{-31} \text{ kg}$	(Electron mass)
$m_p = 1.67 \times 10^{-27} \text{ kg}$	(Proton mass)

Prefixes of units

$m = 10^{-3}$	$\mu = 10^{-6}$	$n = 10^{-9}$	$p = 10^{-12}$
$k = 10^3$	$M = 10^6$	$G = 10^9$	$T = 10^{12}$

For use by Instructors only

Problems	1	2	3	4	5	6	Questions	Total
Marks								

Instructions to the Students:

1. Mobile or other electronic devices are **strictly prohibited** during the exam.
2. Programmable calculators, which can store equations, are not allowed.
3. Cheating incidents will be processed according to the university rules.

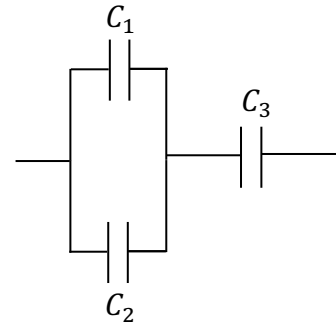
PART I: Solve the following problems. Show your solutions in detail.

1. In the given network of capacitors, $C_1 = 5 \text{ nF}$ and $C_2 = 15 \text{ nF}$. The total electric energy stored in the network is 32 nJ , and the total electric charge is 16 nC . Find the capacitance C_3 . **[4 points]**

$$U_{total} = \frac{1}{2} \frac{Q_{total}^2}{C_{eq}} \Rightarrow C_{eq} = 4 \text{ nF}$$

$$C_{12} = C_1 + C_2 \Rightarrow C_{12} = 20 \text{ nF}$$

$$\frac{1}{C_{eq}} = \frac{1}{C_{12}} + \frac{1}{C_3} \Rightarrow C_3 = 5 \text{ nF}$$



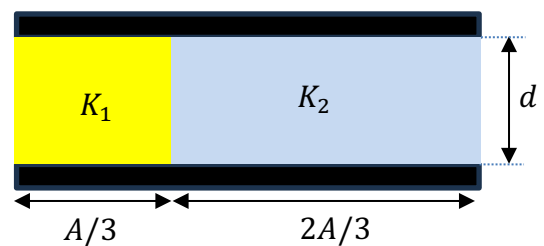
2. An air-filled parallel-plate capacitor with surface area A and plate separation d , has capacitance $C_0 = 15 \text{ nF}$. Then, the capacitor is filled with a dielectric slab of dielectric constant $K_1 = 3$ filling $1/3$ of the space between the plates, and a slab of dielectric constant $K_2 = 5$ filling $2/3$ of the space between the plates, as shown. Calculate the capacitance of this capacitor. **[3 points]**

$$C_0 = \epsilon_0 \frac{A}{d}$$

$$C_1 = K_1 \epsilon_0 \frac{A/3}{d} \Rightarrow C_1 = C_0 \Rightarrow C_1 = 15 \text{ nF}$$

$$C_2 = K_2 \epsilon_0 \frac{2A/3}{d} \Rightarrow C_2 = \frac{10}{3} C_0 \Rightarrow C_2 = 50 \text{ nF}$$

$$C_{eq} = C_1 + C_2 \Rightarrow C_{eq} = 65 \text{ nF}$$



3. A cylindrical aluminum wire with length $L = 5 \text{ cm}$ is connected to a battery which produces an electric field of magnitude E . The aluminum has resistivity $\rho = 2.75 \times 10^{-8} \text{ } \Omega \cdot \text{m}$ and concentration of moving charges is $n = 1.81 \times 10^{29} \text{ m}^{-3}$. The average travel time of the electrons along the length of the wire is 4.5 mins. Find the magnitude of the electric field E . [3 points]

$$v_d = \frac{L}{\Delta t} \Rightarrow v_d = 1.85 \times 10^{-4} \text{ m/s}$$

$$J = nqv_d \Rightarrow J = 5.36 \times 10^6 \text{ A/m}^2$$

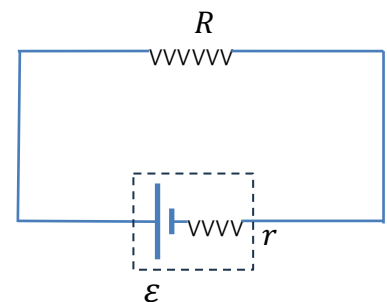
$$E = \rho J \Rightarrow E = 0.15 \text{ V/m}$$

4. In the circuit below, the **terminal voltage** across the battery is 15 V. The power dissipated on resistor R is 25 W. The internal resistance of the battery is $0.6 \text{ } \Omega$. Calculate the electromotive force ε of the battery. [3 points]

$$P_R = \frac{V_{term}^2}{R} \Rightarrow R = \frac{V_{term}^2}{P_R} \Rightarrow R = 9 \text{ } \Omega$$

$$I = \frac{V_{term}}{R} \Rightarrow I = 1.67 \text{ A}$$

$$V_{term} = \varepsilon - Ir \Rightarrow \varepsilon = V_{term} + Ir \Rightarrow \varepsilon = 16 \text{ V}$$



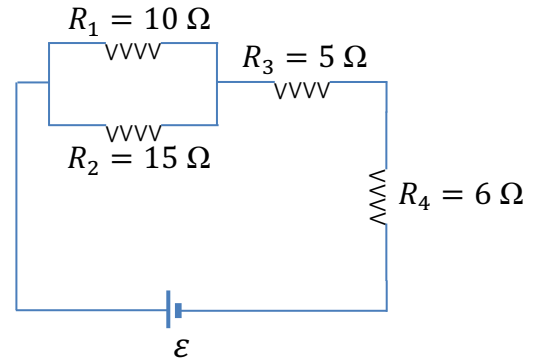
5. In the circuit shown below, the electric current through resistor R_4 is 2 A. Find the power dissipated on resistor R_1 . [4 Points]

$$I = I_4 = 2 \text{ A}$$

$$\frac{1}{R_{12}} = \frac{1}{R_1} + \frac{1}{R_2} \Rightarrow R_{12} = 6 \Omega$$

$$V_{12} = IR_{12} \Rightarrow V_{12} = 12 \text{ V}$$

$$P_1 = \frac{(V_{12})^2}{R_1} \Rightarrow P_1 = 14.4 \text{ W}$$



6. Find the electric currents I_1 , I_2 , I , and the potential difference V_{ac} in the circuit below. [5 Points]

Junction rule: $I = I_1 + I_2$ (1)

Loop rules:

Upper loop (acba)

$$8 + 5I_2 - 3I - 2I = 0 \Rightarrow$$

$$8 - 5I_1 - 10I_2 = 0 \quad (2)$$

Big loop (abcd)

$$10 + 5I_2 - 8 - 4I_1 = 0 \Rightarrow 2 - 4I_1 + 5I_2 = 0 \quad (3)$$

Multiply (2) with 4 and (3) with (-5), then subtract them.

$$I_1 = 0.923 \text{ A} \quad (4)$$

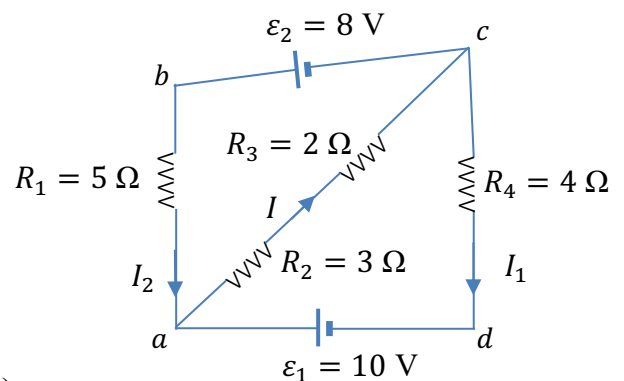
From (3), we get:

$$I_2 = 0.338 \text{ A}$$

From (1), we get:

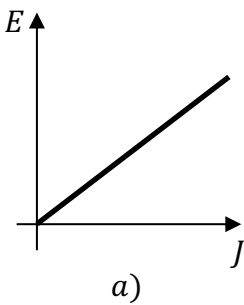
$$I = 1.261 \text{ A}$$

$$V_a - 5I = V_c \Rightarrow V_{ac} = 6.31 \text{ V}$$

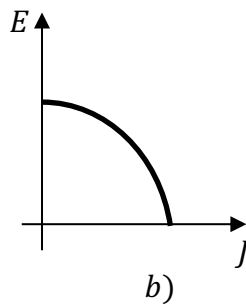


PART II: Conceptual Questions (each carries 1 point). Tick the best answer:

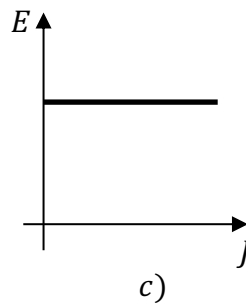
- Which statement is correct?
 - The capacitor is a device that stores electric current and electric potential energy.
 - The capacitor is a device that stores electric charge and electric potential energy. **(ANSWER)**
 - The capacitor is a device that stores electric charge and electric current.
 - The capacitor is a device that absorbs electric charge and electric potential energy.
- An air-filled parallel-plate capacitor with plate separation d , area A , and capacitance C is charged by a battery V . Then the battery is disconnected and a slab of dielectric material is inserted completely filling the space between the plates of the capacitor. The electric potential energy of the capacitor will
 - remain the same.
 - increase.
 - decrease. **(ANSWER)**
 - be zero.
- Which diagram shows the magnitude of the electric field versus the current density (E vs J) of a metallic wire?



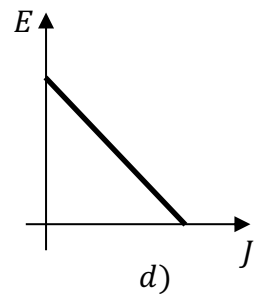
a)



b)



c)



d)

(ANSWER)

- The Kirchhoff 's junction rule is a consequence of the
 - conservation of electric potential energy.
 - conservation of electric charge. **(ANSWER)**
 - conservation of mechanical energy.
 - conservation of momentum.

5. Applying the Kirchhoff's loop rule in a closed loop, we must travel the closed loop

- a) only clockwise
- b) only counter-clockwise
- c) either clockwise or counter-clockwise. **(ANSWER)**
- d) based on the polarity of the source of emf.

6. In a network of resistors, there are 10 identical resistors of resistance R each one of them. The total resistance of this network is maximized when

- a) all the 10 resistors are connected in parallel.
- b) 5 resistors in series followed by 5 resistors in parallel.
- c) all the 10 resistors are connected in series. **(ANSWER)**
- d) none of the above.