



**Final Examination**  
**Fall Semester 2025 – 2026**

**December 28, 2025**  
**Time: 6:00 – 8:00 PM**

Name: ..... Student No: .....

Section No: ..... Serial No: .....

Instructors: Drs. Ali, Al-Mumin, Lajko, Sharma & Vagenas

**Fundamental constants**

$$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ N.m}^2/\text{C}^2 \quad (\text{Coulomb constant})$$

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N} \cdot \text{m}^2) \quad (\text{Permittivity of free space})$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ T} \cdot \text{m/A} \quad (\text{Permeability of free space})$$

$$|e| = 1.60 \times 10^{-19} \text{ C} \quad (\text{Elementary unit of charge})$$

$$N_A = 6.02 \times 10^{23} \quad (\text{Avogadro's number})$$

$$g = 9.8 \text{ m/s}^2 \quad (\text{Acceleration due to gravity})$$

$$m_e = 9.11 \times 10^{-31} \text{ kg} \quad (\text{Electron mass})$$

$$m_p = 1.67 \times 10^{-27} \text{ kg} \quad (\text{Proton mass})$$

**Prefixes of units**

$$\begin{array}{ll} m = 10^{-3} & \mu = 10^{-6} \\ k = 10^3 & M = 10^6 \end{array}$$

$$\begin{array}{ll} n = 10^{-9} & p = 10^{-12} \\ G = 10^9 & T = 10^{12} \end{array}$$

**For use by Instructors only**

Problems	1	2	3	4	5	6	7	8	9	10	Questions	Total
Marks												

**Instructions to the Students:**

1. Mobile or other electronic devices are **strictly prohibited** during the exam.
2. Programmable calculators, which can store equations, are not allowed.
3. Cheating incidents will be processed according to the university rules.

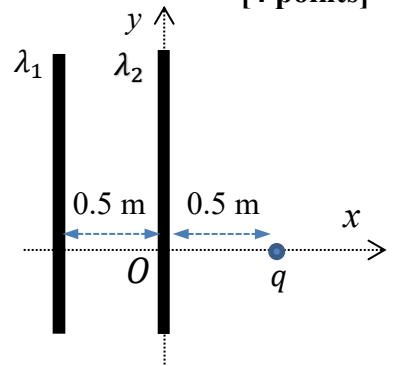
**PART I: Solve the following problems. Show your solutions in detail.**

1. Two very long uniformly charged lines with  $\lambda_1 = -12 \text{ } \mu\text{C/m}$ ,  $\lambda_2 = 18 \text{ } \mu\text{C/m}$  are placed parallel with the  $y$ -axis, as shown. A particle of charge  $q = -4 \text{ } \mu\text{C}$  and mass  $m = 4 \times 10^{-3} \text{ kg}$  is released on the  $x$ -axis as shown. Calculate the acceleration vector  $\vec{a}$  of  $q$ . [4 points]

$$\vec{E} = \frac{\lambda_1}{2\pi\epsilon_0 1m} \hat{i} + \frac{\lambda_2}{2\pi\epsilon_0 0.5m} \hat{i} = 4.32 \times 10^5 \frac{\text{N}}{\text{C}} \hat{i}$$

$$\vec{F} = q\vec{E} = -(1.73 \text{ N})\hat{i}$$

$$\vec{a} = \frac{\vec{F}}{m} = -(432.5 \frac{\text{m}}{\text{s}^2})\hat{i}$$

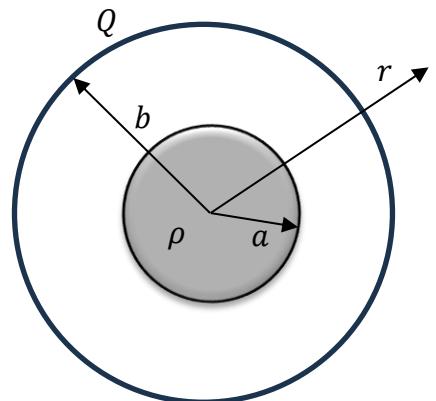


2. A sphere of radius  $a = 5 \text{ cm}$  with a uniform volume charge density  $\rho = -3 \text{ } \mu\text{C/m}^3$  is inside a concentric thin conducting spherical shell of radius  $b = 10 \text{ cm}$  and charge  $Q = 1.26 \text{ nC}$ . Calculate the magnitude and direction of the net electric field  $\vec{E}$  at  $r = 12 \text{ cm}$ . [3 points]

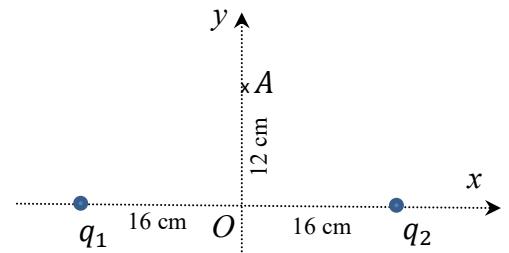
$$\text{Gauss's Law: } \oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0} \Rightarrow E(4\pi r^2) = \frac{Q_{encl}}{\epsilon_0}$$

$$Q_{encl} = \rho \frac{4\pi}{3} a^3 + Q = -0.311 \text{ nC}$$

$$E = \frac{Q_{encl}}{\epsilon_0 4\pi r^2} = -194.2 \text{ N/C, inward}$$



3. Two charges  $q_1 = q_2 = 12 \mu\text{C}$  are fixed on the  $x$ -axis, as shown. A third charge  $q_3 = -4 \mu\text{C}$  with mass  $m = 0.05 \text{ kg}$  is released from rest at point  $A$ . Calculate the speed of  $q_3$  at point  $O$ . [3 points]



Mechanical Energy conservation:

$$U_{q_3}^A = U_{q_3}^O + K_{q_3}^O = U_{q_3}^O + \frac{m}{2}v^2$$

$$U_{q_3}^A = q_3(V_A^1 + V_A^2) = q_3 \left( k \frac{q_1}{0.2 \text{ m}} + k \frac{q_2}{0.2 \text{ m}} \right) = -4.32 \text{ J}$$

$$U_{q_3}^O = q_3(V_O^1 + V_O^2) = q_3 \left( k \frac{q_1}{0.16 \text{ m}} + k \frac{q_2}{0.16 \text{ m}} \right) = -5.4 \text{ J}$$

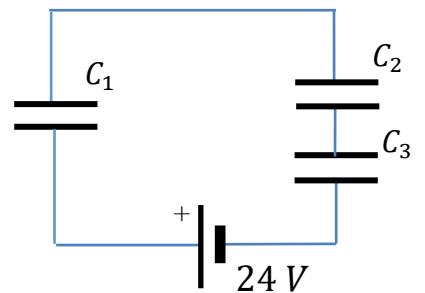
$$U_{q_3}^A - U_{q_3}^O = \frac{m}{2}v^2 \Rightarrow v = 6.57 \text{ m/s}$$

4. A network of capacitors  $C_1 = 4 \mu\text{F}$ ,  $C_2 = 6 \mu\text{F}$ , and  $C_3 = 12 \mu\text{F}$ , is charged by a battery, as shown. Determine the potential difference across  $C_2$ . [3 points]

$$C_{eq} = \left( \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3} \right)^{-1} = 2 \mu\text{F}$$

$$Q = C_{eq}V = 48 \mu\text{C} \quad Q_2 = Q$$

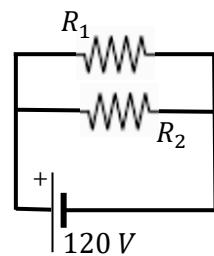
$$\text{so } V_2 = \frac{Q}{C_2} = 8 \text{ V}$$



5. Two resistors,  $R_1 = 20 \Omega$  and  $R_2$ , are connected across a 120-V emf device as shown so that 16 A current flows through the emf device. What is the value of  $R_2$ ? [3 points]

$$R_{eq} = \frac{V}{I} = 7.5 \Omega$$

$$R_{eq} = \frac{R_1 \cdot R_2}{R_1 + R_2} \Rightarrow R_2 = 12 \Omega$$



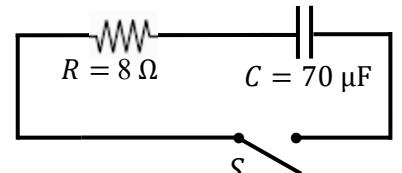
6. In the circuit below, the capacitor has an initial charge  $Q_0 = 400 \mu\text{C}$ . The switch  $S$  is closed at  $t = 0$ . Calculate the current in the circuit at the time when the energy stored in the capacitor is  $\frac{1}{9}$  of its initial value. [4 points]

$$q(t) = Q_0 e^{-\frac{t}{RC}} \Rightarrow U = \frac{Q_0^2 (e^{-\frac{t}{RC}})^2}{2C} = U_0 e^{-\frac{2t}{RC}}$$

$$\frac{U_0}{9} = U_0 e^{-2t_1/RC} \Rightarrow e^{-t_1/RC} = \frac{1}{3}$$

$$\Rightarrow I = -\frac{dq}{dt} = \frac{Q_0}{RC} e^{-t_1/RC}$$

$$I = \frac{Q_0}{RC} e^{-\frac{t_1}{RC}} = \frac{Q_0}{RC} \frac{1}{3} = 0.24 \text{ A}$$



7. A particle of charge  $q = 4 \text{ C}$  enters a region of uniform electric and uniform magnetic fields with initial velocity  $\vec{v} = (6 \text{ m/s})\hat{i}$ . The uniform magnetic field is  $\vec{B} = (0.5 \text{ T})\hat{i} + (2.0 \text{ T})\hat{j}$  and the net initial force on the particle is  $\vec{F} = (12 \text{ N})\hat{i} + (16 \text{ N})\hat{k}$ . Find the uniform electric field  $\vec{E}$ . **[3 points]**

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B} \Rightarrow \vec{E} = \frac{\vec{F} - q\vec{v} \times \vec{B}}{q}$$

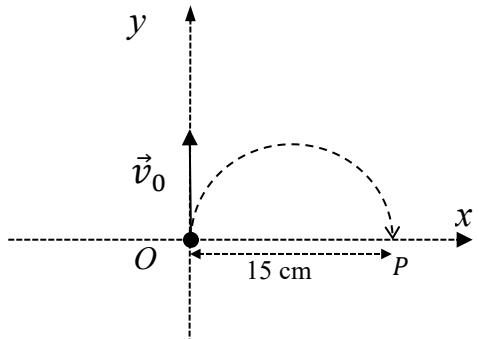
$$\vec{E} = \left(3 \frac{\text{N}}{\text{C}}\right)\hat{i} - \left(8 \frac{\text{N}}{\text{C}}\right)\hat{k}$$

8. An electron at point  $O$  has a velocity  $\vec{v}_0 = (1.6 \times 10^6 \frac{\text{m}}{\text{s}})\hat{j}$ . Find the magnitude and the direction of the magnetic field that will cause the electron to follow the semi-circular path from  $O$  to  $P$ . **[3 points]**

$$R = \frac{0.15 \text{ m}}{2} = 0.075 \text{ m}$$

$$R = \frac{mv_{\perp}}{|q|B} \Rightarrow B = \frac{mv_{\perp}}{|q|R} = 1.21 \times 10^{-4} \text{ T}$$

*Direction is into the page or  $-\hat{k}$ .*

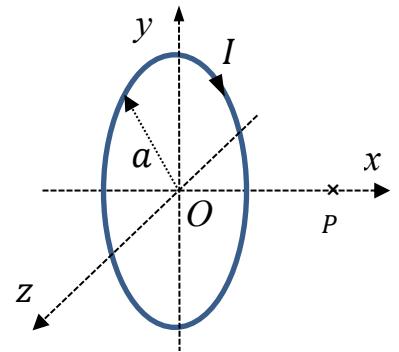


9. A circular current loop centred at the origin has radius  $a = 10 \text{ cm}$  and current  $I = 5 \text{ A}$ . The symmetry axis of the loop is the  $x$ -axis. If at point  $P$ , shown in the figure, the magnitude of the magnetic field is  $\frac{1}{2}$  of that at the origin, find the distance of point  $P$  from the origin. **[3 points]**

$$B_P = \frac{1}{2} B_O$$

$$\frac{\mu_0 I a^2}{2(x^2+a^2)^{3/2}} = \frac{1}{2} \frac{\mu_0 I a^2}{2a^3}$$

$$x = 0.0766 \text{ m}$$



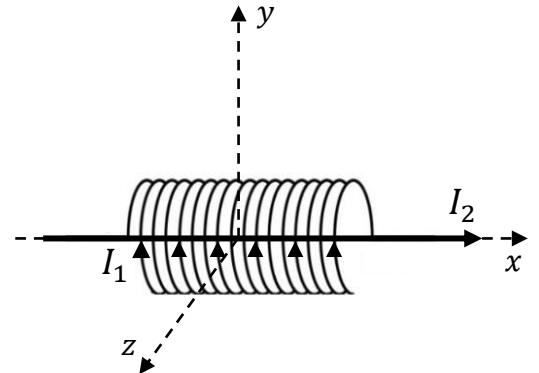
10. A 2-m long solenoid has 3000 turns, radius 6 cm, and current  $I_1 = 20 \text{ mA}$ . The solenoid is placed on the  $x$ -axis, as shown. A very long straight wire is inserted along the  $x$ -axis with current  $I_2 = 6 \text{ A}$ . Find the magnitude of the net magnetic field at 2 cm distance from the origin on the  $+y$ -axis. **[3 points]**

$$\vec{B}_1 = -\mu_0 n I_1 \hat{i} = -(3.77 \times 10^{-5} \text{ T}) \hat{i}$$

$$\vec{B}_2 = \frac{\mu_0 I_2}{2\pi d} \hat{k} = (6 \times 10^{-5} \text{ T}) \hat{k}$$

$$\vec{B} = \vec{B}_1 + \vec{B}_2$$

$$B = \sqrt{B_1^2 + B_2^2} = 7.09 \times 10^{-5} \text{ T}$$



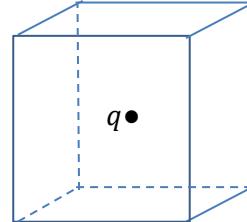
**PART II: Conceptual Questions (each carries 1 point). Tick the best answer:**

1. If two charged particles, with  $q$  charge on each, are separated by a distance  $d$ , the magnitude of the force between them is  $F$ . What is the magnitude of the force between them if each charge is doubled and the separation changes to  $d/2$ ?

- a)  $F$ .
- b)  $4F$ .
- c)  $16F$ . 
- d)  $F/4$ .

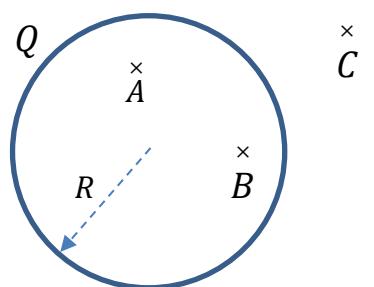
2. A point charge  $q$  is placed at the centre of a cube, as shown. What is the electric flux through one face of the cube?

- a)  $\frac{q}{\epsilon_0}$ .
- b)  $\frac{q}{2\epsilon_0}$ .
- c)  $\frac{q}{3\epsilon_0}$ .
- d)  $\frac{q}{6\epsilon_0}$ . 



3. A conducting sphere with charge  $Q > 0$  has radius  $R$ . At the points  $A$ ,  $B$ , and  $C$  the electric potential is  $V_A$ ,  $V_B$ , and  $V_C$ , respectively. Which relation is correct?

- a)  $V_A = V_C$ .
- b)  $V_B = V_C$ .
- c)  $V_A < V_C$ .
- d)  $V_B > V_C$ . 



4. If  $N$  identical capacitors, each have capacitance  $C$ , are connected in series. The equivalent capacitance of this network is

- a)  $C/N$ . 
- b)  $NC$ .
- c)  $N^2C$ .
- d)  $C$ .

5. If a current through a resistor is increased by a factor of 2, the dissipated power

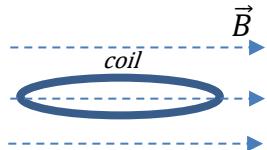
- a) decreases by a factor of 2.
- b) increases by a factor of 2.
- c) decreases by a factor of 4.
- d) increases by a factor of 4. 

6. In an  $R-C$  circuit after the switch is closed at time  $t = 0$ , the current will be  $\frac{1}{e}$  of its initial value at  $t_1 = \tau$ . The current will be  $\frac{1}{e^2}$  of its initial value at

- a)  $t_2 = \tau/2$ .
- b)  $t_2 = 2\tau$ . 
- c)  $t_2 = \tau^2$ .
- d)  $t_2 = 2\tau^2$ .

7. A coil is placed in a magnetic field so that the plane of the coil is parallel to the direction of the magnetic field. The magnitude of the magnetic flux through the coil can be changed

- a) by changing the magnitude of the magnetic field.
- b) by changing the area of the coil.
- c) by changing the angle between the direction of the magnetic field and the plane of the coil. 
- d) by reversing the magnetic field direction suddenly without changing its magnitude.



8. Two parallel wires carrying currents  $I_1$ , and  $I_2$  are in the  $xy$ -plane as shown. On the  $x$ -axis, the magnitude of the net magnetic field can be zero

- a) in region  $A$ .
- b) in region  $B$ . 
- c) in region  $C$ .
- d) in none of the regions.

