



**Second Midterm Examination
Fall Semester 2025 - 2026**

November 29, 2025

Time: 11:00 AM – 12:30 PM

Name: Student No:

Section No: Serial No:

Instructors: Drs. Abdul Mohsen, Yahya, Lajko, Sharma, & Vagenas

Fundamental constants

$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ N.m}^2 / \text{C}^2$	(Coulomb constant)
$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N} \cdot \text{m}^2)$	(Permittivity of free space)
$\mu_0 = 4\pi \times 10^{-7} \text{ T.m/A}$	(Permeability of free space)
$ e = 1.60 \times 10^{-19} \text{ C}$	(Elementary unit of charge)
$N_A = 6.02 \times 10^{23}$	(Avogadro's number)
$g = 9.8 \text{ m/s}^2$	(Acceleration due to gravity)
$m_e = 9.11 \times 10^{-31} \text{ kg}$	(Electron mass)
$m_p = 1.67 \times 10^{-27} \text{ kg}$	(Proton mass)

Prefixes of units

$m = 10^{-3}$	$\mu = 10^{-6}$	$n = 10^{-9}$	$p = 10^{-12}$
$k = 10^3$	$M = 10^6$	$G = 10^9$	$T = 10^{12}$

For use by Instructors only

Problems	1	2	3	4	5	6	7	8	Questions	Total
Marks										

Instructions to the Students:

1. Mobile or other electronic devices are **strictly prohibited** during the exam.
2. Programmable calculators, which can store equations, are not allowed.
3. Cheating incidents will be processed according to the university rules.

PART I: Solve the following problems. Show your solutions in detail.

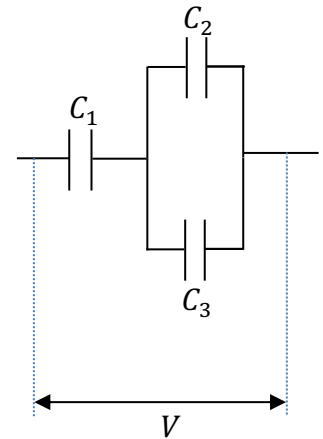
1. In the given network of capacitors with $C_1 = 30 \text{ nF}$ and $C_2 = C_3 = 10 \text{ nF}$, the charge on capacitor C_1 is $Q_1 = 60 \text{ nC}$. Find the electric energy stored in the network. **[4 points]**

$$C_{23} = C_2 + C_3 \Rightarrow C_{23} = 20 \text{ nF}$$

$$\frac{1}{C_{123}} = \frac{1}{C_1} + \frac{1}{C_{23}} \Rightarrow C_{123} = 12 \text{ nF}$$

$$Q_1 = Q_{23} = Q_{total} = 60 \text{ nC}$$

$$U_{total} = \frac{1}{2} \frac{Q_{total}^2}{C_{123}} \Rightarrow U_{total} = 150 \text{ nJ}$$



2. A capacitor $C_1 = 15 \mu\text{F}$ is charged by a source of emf $\varepsilon = 6 \text{ V}$. Then, the switch S is placed to position 2. The capacitor $C_2 = 30 \mu\text{F}$ is uncharged initially. Find the final electric charge stored in C_2 . **[4 points]**

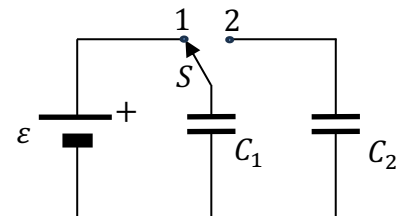
Position 1: $Q = C_1 \varepsilon \Rightarrow Q = 90 \mu\text{C}$

Position 2: $C_{12} = C_1 + C_2 \Rightarrow C_{12} = 45 \mu\text{F}$

$$V = \frac{Q}{C_{12}} \Rightarrow V = 2 \text{ V}$$

$$V = V_1 = V_2 = 2 \text{ V}$$

$$C_2 = \frac{Q_2}{V_2} \Rightarrow Q_2 = C_2 V_2 \Rightarrow Q_2 = 60 \mu\text{C}$$



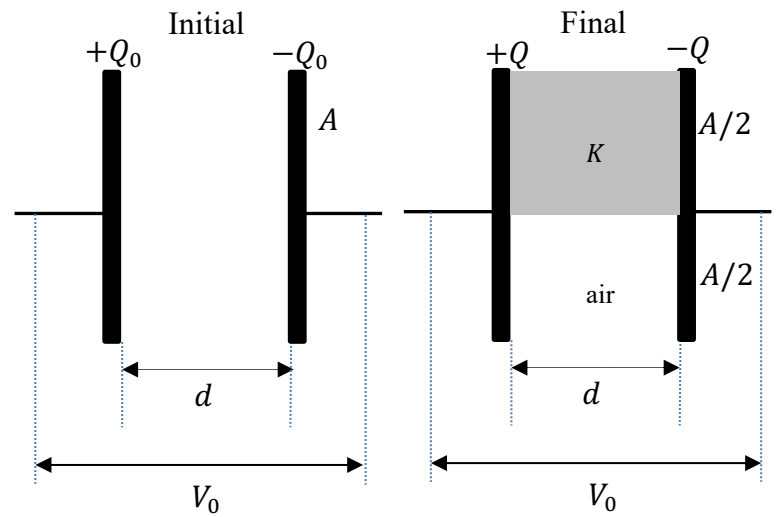
3. An air-filled parallel-plate capacitor with a surface area A , a plate separation d , and capacitance C_0 is charged by a battery V_0 and its initial charge is $Q_0 = 15 \text{ nC}$. Then, while the battery remains connected, the capacitor is half filled with a dielectric material of dielectric constant $K = 4$, as shown. What is the new capacitance? [4 points]

$$C_0 = \frac{Q_0}{V_0} \quad \text{and} \quad C_0 = \epsilon_0 \frac{A}{d}$$

$$C_{\text{air}} = \epsilon_0 \frac{A/2}{d} \Rightarrow C_{\text{air}} = 0.5C_0$$

$$C_{\text{diel}} = K\epsilon_0 \frac{A/2}{d} \Rightarrow C_{\text{diel}} = 2C_0$$

$$C_{\text{eq}} = C_{\text{air}} + C_{\text{diel}} \Rightarrow C_{\text{eq}} = 2.5C_0$$



4. A conductor has variable square cross-section as shown. The electric current in the conductor is steady, and the drift speed of the electrons at the cross-section 1 is $9.2 \times 10^{-4} \text{ m/s}$. Find the drift speed at the cross-section 2. [4 points]

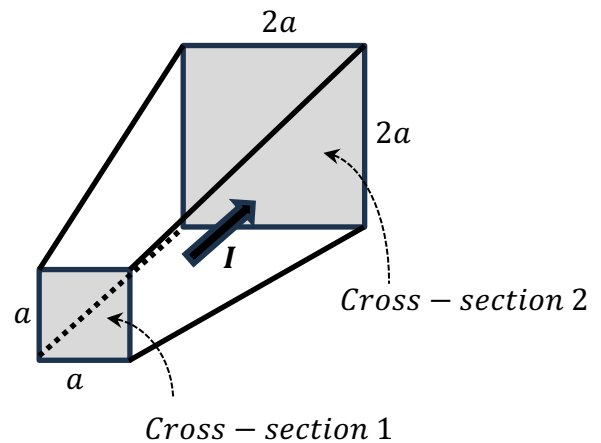
$$I_1 = I_2 = I$$

$$J_1 A_1 = J_2 A_2$$

$$n|q|v_{d1}a^2 = n|q|v_{d2}(2a)^2$$

$$v_{d1} = 4v_{d2} \Rightarrow v_{d2} = \frac{v_{d1}}{4}$$

$$v_{d2} = 2.3 \times 10^{-4} \text{ m/s}$$



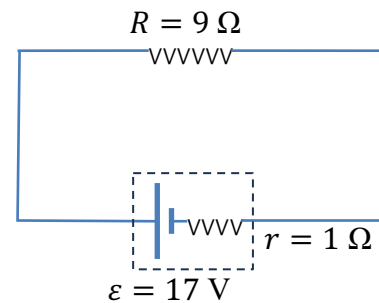
5. In the circuit below, calculate the total energy dissipated in the resistor with resistance R in a time period of 3 minutes. [4 points]

$$IR = \varepsilon - Ir \Rightarrow I = \frac{\varepsilon}{R+r} \Rightarrow I = 1.7 \text{ A}$$

$$P_R = I^2 R \Rightarrow P_R = 26 \text{ W}$$

$$P_R = \frac{U}{\Delta t} \Rightarrow U = P_R \Delta t$$

$$U = 26 \times 180 \text{ J} \Rightarrow U = 4,681 \text{ J}$$



6. In the circuit below, the potential difference between a and b is 39 V, find the source of emf ε_2 .

[4 Points]

$$V_a + 5I + 4I - 57 = V_b$$

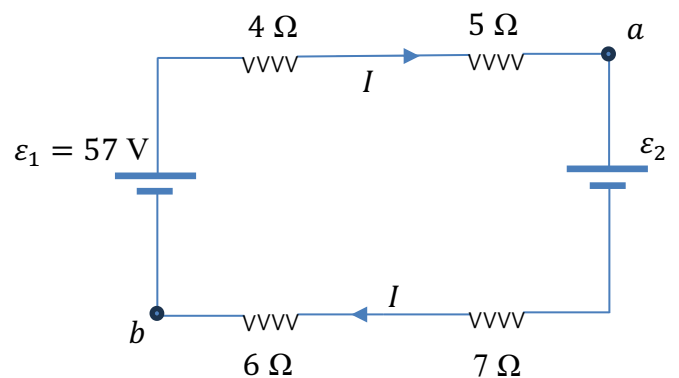
$$V_a - V_b + 9I = 57 \Rightarrow 39 + 9I = 57$$

$$I = 2 \text{ A}$$

Loop rule:

$$\varepsilon_1 - 4I - 5I - \varepsilon_2 - 7I - 6I = 0$$

$$\varepsilon_2 = \varepsilon_1 - 22I \Rightarrow \varepsilon_2 = 13 \text{ V}$$



7. Find the electric currents I_1 , I_2 , and I in the circuit below.

[4 Points]

Junction rule: $I = I_1 + I_2$

Loop rules:

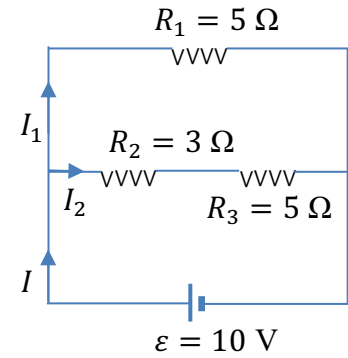
Lower loop

$$10 - 3I_2 - 5I_2 = 0 \Rightarrow I_2 = 1.25 \text{ A}$$

Big loop

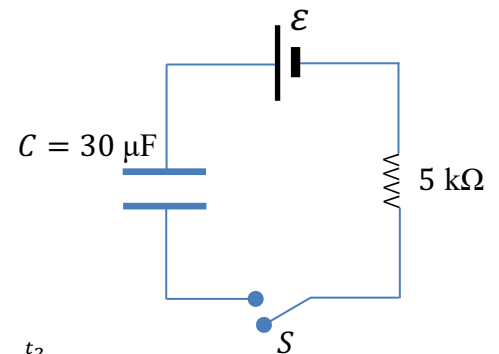
$$10 - 5I_1 = 0 \Rightarrow I_1 = 2 \text{ A}$$

$$I = I_1 + I_2 \Rightarrow I = 3.25 \text{ A}$$



8. In the RC circuit below, the switch S is closed at time $t = 0$ s. At time t_1 , the charge of the capacitor is $90 \mu\text{C}$ and the electric current in the circuit is 1 mA . Find the electric current in the circuit at the time $t_2 = 100 \mu\text{s}$.

[4 Points]



At time t_1 , apply loop rule:

$$\varepsilon - i(t_1)R - \frac{q(t_1)}{C} = 0$$

$$\varepsilon - (5 \times 10^3) \times (1 \times 10^{-3}) - \frac{90 \times 10^{-6}}{30 \times 10^{-6}} = 0 \Rightarrow \varepsilon = 8 \text{ V}$$

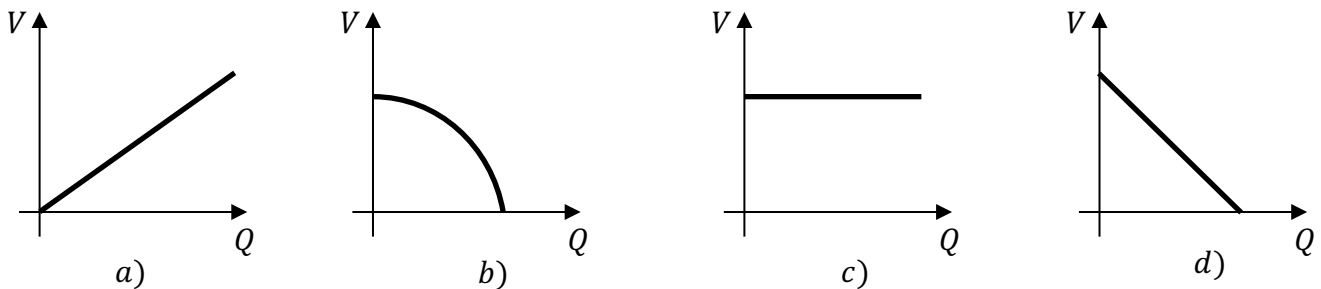
$$i(t) = \frac{dq}{dt} \Rightarrow i(t) = \frac{Q}{RC} e^{-\frac{t}{RC}} \Rightarrow i(t_2) = \frac{Q}{RC} e^{-\frac{t_2}{RC}} \Rightarrow i(t_2) = \frac{\varepsilon}{R} e^{-\frac{t_2}{RC}}$$

$$i(t_2) = 1.6 \text{ mA}$$

PART II: Conceptual Questions (each carries 1 point). Tick the best answer:

1. Which statement is correct? The capacitance of a capacitor depends on
- a) the charge of the capacitor.
 - b) the potential difference between the plates of the capacitor.
 - c) the geometry of the capacitor and the matter between its plates. **(ANSWER)**
 - d) all the above.
2. An air-filled parallel-plate capacitor with plate separation d , area A , and capacitance C is charged by a battery V and the battery remains connected. Then a slab of dielectric material is inserted completely filling the space between the plates of the capacitor. The electric energy density will
- a) remain the same.
 - b) increase. **(ANSWER)**
 - c) decrease.
 - d) be zero.

3. Which diagram shows the potential difference versus electric charge (V vs Q) in a capacitor?

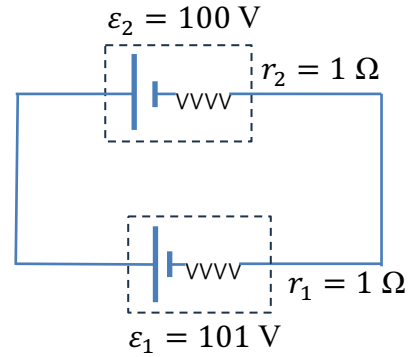


(ANSWER)

4. The value of the resistance R of a cylindrical conductor depends on
- a) the material of the conductor.
 - b) the length of the conductor.
 - c) the area of the cross-section of the conductor.
 - d) all the above. **(ANSWER)**

5. In the circuit below, the terminal voltage across the upper battery is:

- a) $V_{term,2} = \varepsilon_2 - Ir_1$.
- b) $V_{term,2} = \varepsilon_2 - Ir_2$.
- c) $V_{term,2} = \varepsilon_2 + Ir_1$.
- d) $V_{term,2} = \varepsilon_2 + Ir_2$. **(ANSWER)**

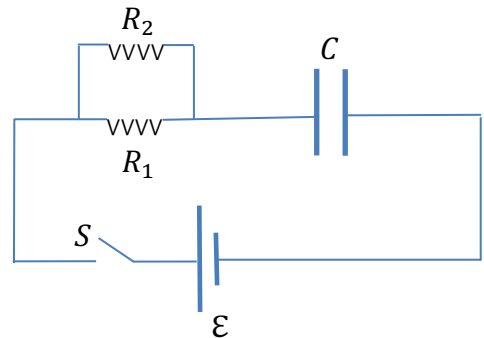


6. If two resistors R_1 and R_2 are connected in parallel and have currents I_1 and I_2 , respectively, what is their relation?

- a) $\frac{I_1}{I_2} = \frac{R_1}{R_2}$.
- b) $\frac{I_1}{I_2} = \frac{R_2}{R_1}$. **(ANSWER)**
- c) $\frac{I_1}{R_1} = \frac{R_2}{I_2}$.
- d) $\frac{I_1}{I_2} = \frac{R_1 R_2}{R_1 + R_2}$.

7. In the RC circuit below, the time constant τ is equal to

- a) $R_1 C$.
- b) $(R_1 + R_2) C$.
- c) $\frac{R_1 + R_2}{R_1 R_2} C$.
- d) $\frac{R_1 R_2}{R_1 + R_2} C$. **(ANSWER)**



8. In an RC circuit, while the capacitor is discharging, the potential difference across the resistance R

- a) remains the same.
- b) decreases exponentially. **(ANSWER)**
- c) increases exponentially.
- d) increases and then decreases.