


 Second Midterm Examination  
Summer Semester 2024 - 2025

July 19, 2025

Time: 1:00 PM – 2:30 PM

Name: ..... Student No: .....

Section No: ..... Serial No: .....

Instructors: Drs. Yahya Al-Munin, Peter Lajko, &amp; Elias Vagenas

**Fundamental constants**

$k = \frac{1}{4\pi\epsilon_0} = 9.0 \times 10^9 \text{ Nm}^2/\text{C}^2$	(Coulomb constant)
$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2 / (\text{N} \cdot \text{m}^2)$	(Permittivity of free space)
$\mu_0 = 4\pi \times 10^{-7} \text{ T.m/A}$	(Permeability of free space)
$ e  = 1.60 \times 10^{-19} \text{ C}$	(Elementary unit of charge)
$N_A = 6.02 \times 10^{23}$	(Avogadro's number)
$g = 9.8 \text{ m/s}^2$	(Acceleration due to gravity)
$m_e = 9.11 \times 10^{-31} \text{ kg}$	(Electron mass)
$m_p = 1.67 \times 10^{-27} \text{ kg}$	(Proton mass)

**Prefixes of units**

$m = 10^{-3}$	$\mu = 10^{-6}$	$n = 10^{-9}$	$p = 10^{-12}$
$k = 10^3$	$M = 10^6$	$G = 10^9$	$T = 10^{12}$

**For use by Instructors only**

Problems	1	2	3	4	5	6	7	8	Questions	Total
Marks										

**Instructions to the Students:**

1. Mobile or other electronic devices are **strictly prohibited** during the exam.
2. Programmable calculators, which can store equations, are not allowed.
3. Cheating incidents will be processed according to the university rules.

**PART I: Solve the following problems. Show your solutions in detail.**

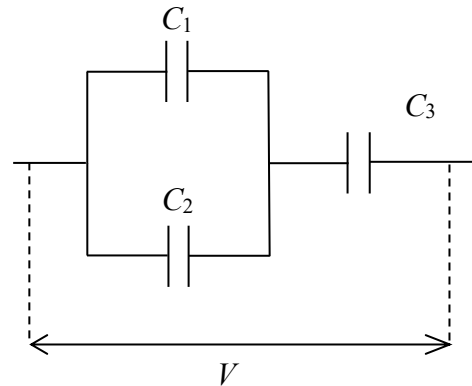
1. In the network of capacitors, with capacitances  $C_1 = 2 \text{ nF}$ ,  $C_2 = 6 \text{ nF}$ ,  $C_3 = 5 \text{ nF}$ , the electric charge stored in the capacitor  $C_1$  is  $Q_1 = 40 \text{ nC}$ . Calculate the electric charge  $Q_3$  stored in the capacitor  $C_3$ .  
**[4 points]**

$$C_1 = \frac{Q_1}{V_1} \Rightarrow V_1 = \frac{Q_1}{C_1} \Rightarrow V_1 = 20 \text{ V}$$

$$C_{12} = C_1 + C_2 \Rightarrow C_{12} = 8 \text{ nF}$$

$$Q_{12} = C_{12}V_1 \Rightarrow Q_{12} = 160 \text{ nC}$$

$$Q_{12} = Q_3 = 160 \text{ nC}$$



2. An air-filled parallel-plate capacitor is charged so that the positively charged plate has surface charge density  $\sigma = 17.7 \text{ } \mu\text{C}/\text{m}^2$ . The volume between the two parallel plates of the conductor is  $2 \times 10^{-5} \text{ m}^3$ . Calculate the electric potential energy stored in the capacitor.  
**[3 points]**

$$E = \frac{\sigma}{\epsilon_0} \Rightarrow E = 2 \times 10^6 \text{ N/C}$$

$$u = \frac{1}{2} \epsilon_0 E^2 \Rightarrow u = 17.7 \text{ J/m}^3$$

$$U = \frac{u}{(\text{volume})} \Rightarrow U = u \times (\text{volume}) \Rightarrow U = 3.54 \times 10^{-4} \text{ J}$$

3. An air-filled parallel-plate capacitor with plate area  $A$  and separation  $d$ , has capacitance  $C_0 = 20 \mu\text{F}$ . The capacitor is partially filled with two dielectric materials of dielectric constant  $K_1 = 3$  and  $K_2$ , as shown. Each dielectric material fills half of the space between the capacitor plates. The capacitance now is  $C = 100 \mu\text{F}$ . Find the dielectric constant  $K_2$ . **[4 points]**

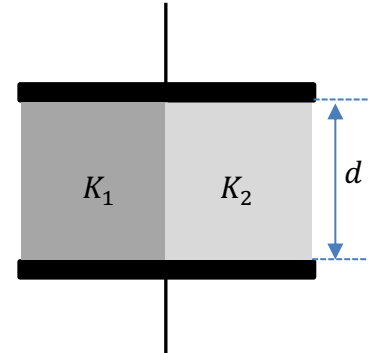
$$C_0 = \epsilon_0 \frac{A}{d}$$

$$C_1 = K_1 \epsilon_0 \frac{A/2}{d} = \frac{K_1}{2} C_0 = 1.5 C_0 = 30 \text{ nF}$$

$$C_2 = K_2 \epsilon_0 \frac{A/2}{d} = \frac{K_2}{2} C_0 = 10 K_2 \text{ nF}$$

$C_1$  and  $C_2$  are in parallel

$$C = C_1 + C_2 \Rightarrow 100 = 30 + 10 K_2 \Rightarrow K_2 = 7$$



4. A cylindrical gold wire with length  $L$  is connected to a battery which produces an electric field inside the wire of magnitude  $E = 25 \text{ N/C}$ . The gold wire has resistivity  $2.44 \times 10^{-8} \Omega \cdot \text{m}$  and concentration of free electrons  $5.90 \times 10^{28} \text{ m}^{-3}$ . If the electrons run the whole length of the wire in time  $\Delta t = 100 \text{ s}$ , calculate the length  $L$  of the gold wire. **[4 points]**

$$E = \rho J \Rightarrow J = \frac{E}{\rho} \Rightarrow J = 1.025 \times 10^9 \text{ A/m}^2$$

$$J = n|q|v_d \Rightarrow v_d = \frac{J}{n|e|} \Rightarrow v_d = 0.109 \text{ m/s}$$

$$v_d = \frac{L}{\Delta t} \Rightarrow L = v_d \Delta t$$

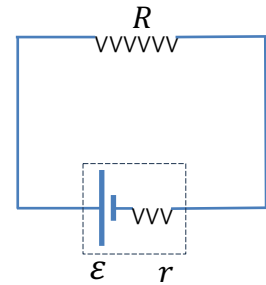
$$L = 10.9 \text{ m}$$

5. In the electric circuit below, the electric current is  $I = 3 \text{ A}$ . The battery has emf of  $10 \text{ V}$  and internal resistance  $r = 1 \Omega$ . Calculate the value of the resistance  $R$ . **[3 points]**

$$V_{term} = \varepsilon - Ir \Rightarrow V_{term} = 7 \text{ V}$$

$$V_{term} = V_R \Rightarrow V_R = 7 \text{ V}$$

$$V_R = IR \Rightarrow R = \frac{V_R}{I} \Rightarrow R = 2.33 \Omega$$



6. In the electric circuit below, the electric current through the resistance  $R_4$  is  $2 \text{ A}$ . Find the electric potential difference  $V_{ab} = V_a - V_b$ . **[5 Points]**

$$V_4 = I_4 R_4 \Rightarrow V_4 = 90 \text{ V}$$

$$R_{23} = R_2 + R_3 \Rightarrow R_{23} = 15 \Omega$$

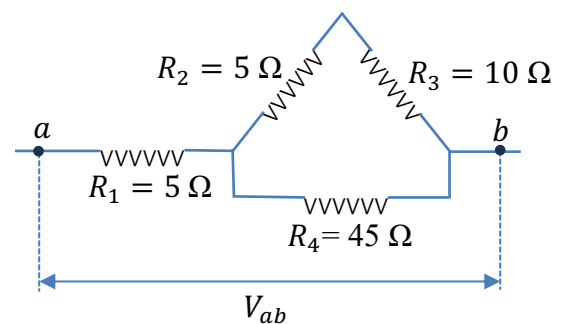
$$V_{23} = V_4 = I_{23} R_{23} \Rightarrow I_{23} = \frac{V_{23}}{R_{23}} \Rightarrow I_{23} = 6 \text{ A}$$

$$I = I_{23} + I_4 \Rightarrow I = 8 \text{ A}$$

$$R_{234} = \frac{R_4 R_{23}}{R_4 + R_{23}} \Rightarrow R_{234} = 11.25 \Omega$$

$$R_{eq} = R_1 + R_{123} \Rightarrow R_{eq} = 16.25 \Omega$$

$$V_{ab} = IR_{eq} \Rightarrow V_{ab} = 130 \text{ V}$$



7. In the circuit below, find the electric currents  $I_1$ , and  $I_2$ .

[5 Points]

**Junction rule:**

$$I_3 = I_1 + I_2$$

**Loop rules:**

**Lower loop**

$$15 + 7I_2 - 13 - 5I_1 = 0 \Rightarrow 2 - 5I_1 + 7I_2 = 0$$

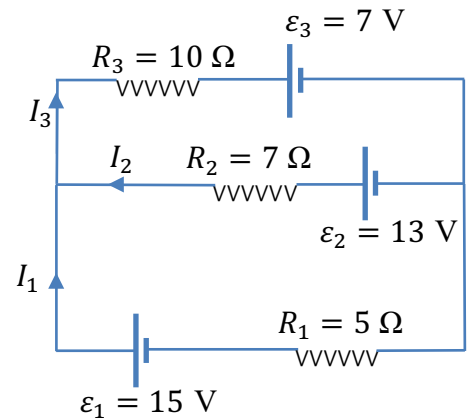
**Upper loop**

$$13 - 7I_2 - 10I_3 - 7 = 0 \Rightarrow 6 - 7I_2 - 10I_3 = 0 \Rightarrow 6 - 10I_1 - 17I_2 = 0$$

Multiply 2<sup>nd</sup> equation with (-2):  $-4 + 10I_1 - 14I_2 = 0$

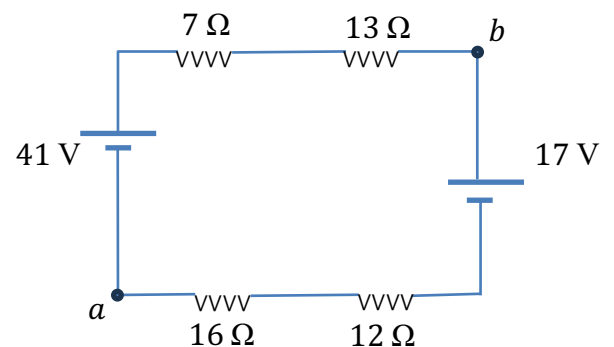
Add the last two questions:  $2 - 31I_2 = 0 \Rightarrow I_2 = 0.065 \text{ A}$

Substitute in the 2<sup>nd</sup> equation to get:  $2 - 5I_1 + 7 \times 0.0645 = 0 \Rightarrow I_1 = 0.491 \text{ A}$



8. In the circuit below, find the potential difference  $V_a - V_b$ .

[4 Points]



**Loop rule:**

$$41 - 7I - 13I - 17 - 12I - 16I = 0$$

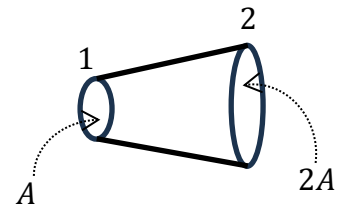
$$24 - 48I = 0 \Rightarrow I = 0.5 \text{ A}$$

$$V_a + 41 - 7I - 13I = V_b$$

$$V_a - V_b = -41 + 20I \Rightarrow V_a - V_b = -31 \text{ V}$$

**PART II: Conceptual Questions (each carries 1 point). Tick the best answer:**

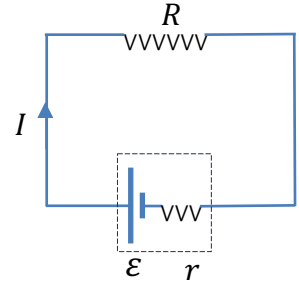
1. In an air-filled parallel-plate capacitor, if the separation between the parallel plates of the capacitor is increased by a factor of 3, and the plate area decreases by a factor of 2, then the capacitance is
  - a) increased by a factor of 3.
  - b) increased by a factor of 6.
  - c) decreased by a factor of 3.
  - d) decreased by a factor of 6. (ANSWER)
  
2. An air-filled parallel-plate capacitor is charged by a battery and then the battery is disconnected. If the capacitor is fully filled with a dielectric constant  $K$ , then the electric energy stored in the capacitor
  - a) increases.
  - b) decreases. (ANSWER)
  - c) remains the same.
  - d) is undetermined.
  
3. A conductor has a variable cross section as shown in the figure. If the drift speed of the moving charges crossing the cross section 1 with cross-sectional area  $A$  is  $v_{d1}$ , then the drift speed of the moving charges crossing the cross section 2 with cross-sectional area  $2A$  is



- a)  $2v_{d1}$ .
  - b)  $4v_{d1}$ .
  - c)  $v_{d1}/2$ . (ANSWER)
  - d)  $v_{d1}/4$ .
- 
4. In conductors, the current density  $\vec{J}$  is directly proportional to the applied electric field  $\vec{E}$ . This relationship is called
    - a) Hooke's law.
    - b) Faraday's law.
    - c) Ohm's law. (ANSWER)
    - d) Gauss's law.

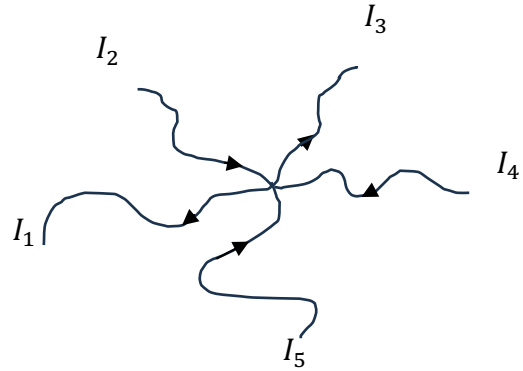
5. For the electric circuit below, the equation  $I^2 R = \varepsilon I - I^2 r$  expresses

- a) the conservation of electric current.
- b) the conservation of electric potential.
- c) the conservation of electric charge.
- d) the conservation of electric energy. (ANSWER)



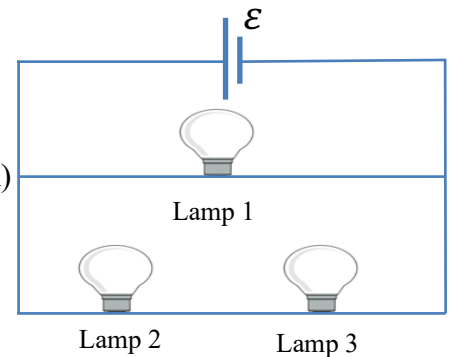
6. Which is the correct junction rule for the junction shown below?

- a)  $I_1 + I_2 - I_3 - I_4 + I_5 = 0$ .
- b)  $I_1 - I_2 + I_3 - I_4 - I_5 = 0$ . (ANSWER)
- c)  $I_1 - I_2 + I_3 - I_4 + I_5 = 0$ .
- d)  $I_1 - I_2 - I_3 + I_4 + I_5 = 0$ .



7. In the electric circuit below, if lamp 3 is removed, then

- a) lamp 1 and lamp 2 will light the same.
- b) lamp 1 will light the same and lamp 2 will light less.
- c) lamp 1 will light the same and lamp 2 will light more. (ANSWER)
- d) lamp 1 and lamp 2 will light more.



8. In the electric circuit below, if  $\varepsilon_2 > \varepsilon_1$ , then the direction of the electric current is

- a) clockwise
- b) counterclockwise (ANSWER)
- c) zero.
- d) undetermined.

